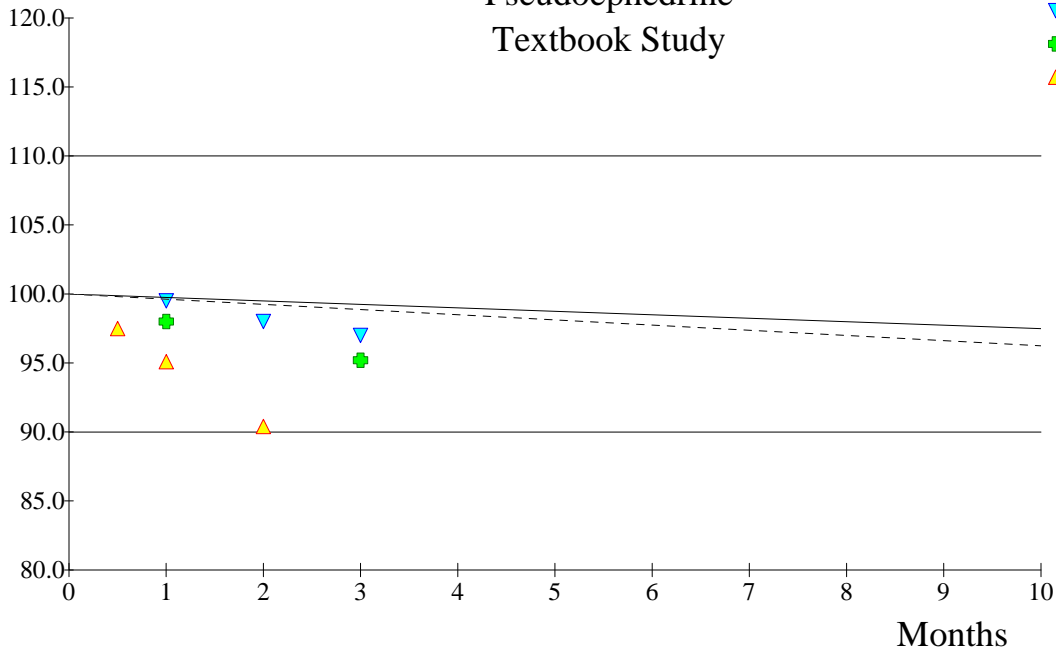


# Shelf Life Projection

Chow and Liu  
Pseudoephedrine  
Textbook Study

Temp. (°C)

Potency



Arrhenius Projection (Zero-Order) at 25.0 °C = 40 Months. Shelf life = 26 Months. (95.0% CI)

Test Category: Assay High Spec: 110.0 Low Spec: 90.0

Test Data

File: C:\Program Files (x86)\SLIM\Demo\Accelerated Conditions.SST User: Craig Hamilton

Zero-Order fit substituted into the Arrhenius equation.

Initial Purity = 100.0 Potency.

Original Raw Data (Time in units of Months):

Temp. (1) 35 °C  
Time : 1.0 2.0 3.0  
Results: 99.50 98.00 97.00

Temp. (2) 45 °C  
Time : 1.0 3.0  
Results: 98.00 95.20

Temp. (3) 55 °C  
Time : 0.5 1.0 2.0  
Results: 97.50 95.10 90.40

Original Raw Data Treatment:

- Less than (<) results are ignored.
- Greater than (>) results are ignored.
- Values that are not between 0.0 and 100.0 are ignored.

Data Points used in Calculations:

Temp. (1) 35 °C  
Time : 1.0 2.0 3.0  
Results: 99.50 98.00 97.00

Temp. (2) 45 °C  
Time : 1.0 3.0  
Results: 98.00 95.20

Temp. (3) 55 °C  
Time : 0.5 1.0 2.0  
Results: 97.50 95.10 90.40

## STATISTICAL ANALYSIS

LOWER ONE-TAILED CONFIDENCE INTERVAL

PROBABILITY LEVEL = 95.0% (equivalent to two-tail 90.0% probability)

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ANOVA Table Under Model  $D(h) = \sum_{ij} \text{Beta}(h)X(h) + e$

| Order of reaction | Source of variation | df | Sum of squares | Mean squares | F value   | p-value | R <sup>2</sup> |
|-------------------|---------------------|----|----------------|--------------|-----------|---------|----------------|
| 0                 | Regression          | 3  | 162.31814      | 54.10605     | 690.37975 | 0.00000 | 99.75917       |
|                   | Residual            | 5  | 0.39186        | 0.07837      |           |         |                |
|                   | Total               | 8  | 162.71000      |              |           |         |                |
| 1                 | Regression          | 3  | 0.01750        | 0.00583      | 778.29613 | 0.00000 | 99.78631       |
|                   | Residual            | 5  | 0.00004        | 0.00001      |           |         |                |
|                   | Total               | 8  | 0.01754        |              |           |         |                |

Zero Order : Product degrades at a constant rate which is independent of concentration.

The Arrhenius equation is  $K = A * \exp(-E/RT)$ , where:  
 K : Rate Constant                    E : Activation Energy  
 A : Frequency Factor                R : Gas Constant (8.31441 J/(K mol))  
 T : Absolute Temperature

Initial estimates using Simple Linear Regression:

A = 7.01506E+012      E = 76479.088

Refined estimates using Taylor series expansion:

A = 3.20451E+013      E = 80545.898

Using the refined estimates, let  $\alpha = \ln(A)$ ,  $\beta = -E/R$ , and  $X = 1/T$ . The Arrhenius equation can be rewritten as  $K = \exp(\alpha + \beta * X)$ , where  $\alpha = 31.098167$  and  $\beta = -9687.506180$ .

Summary of Residuals for Lack of Fit for the Arrhenius Equation

| Source of variation     | df | Sum of squares | Mean squares | F value  | p-value |
|-------------------------|----|----------------|--------------|----------|---------|
| Residual from Arrhenius | 6  | 2.09523        |              |          |         |
| Residual from Model     | 5  | 0.39186        | 0.07837      |          |         |
| Lack of Fit             | 1  | 1.70337        |              | 21.73461 | 0.00552 |

Additional Statistics...

Sum of Squares of the Error = 0.341060  
 Variance of A = 4.583206  
 Variance of b = 489670.277601  
 Variance in K = 0.042960

Zero Order Results:

(By convention, projections are rounded and expiration dates are truncated.)  
 Arrhenius Projection at 25.0 °C = 40 Months.  
 Expiration Date (95.0% CI) at 25.0 °C = 26 Months.

First Order: Product degrades at a constant rate that is proportional to the log of the concentration.

The Arrhenius equation is  $K = A * \exp(-E/RT)$ , where:  
 K : Rate Constant                    E : Activation Energy  
 A : Frequency Factor                R : Gas Constant (8.31441 J/(K mol))  
 T : Absolute Temperature

Initial estimates using Simple Linear Regression:

A = 9.81508E+010      E = 77317.544

Refined estimates using Taylor series expansion:

A = 4.76832E+011      E = 81551.079

Using the refined estimates, let  $\alpha = \ln(A)$ ,  $\beta = -E/R$ , and  $X = 1/T$ . The Arrhenius equation can be rewritten as  $\ln(K) = \alpha + \beta * X$ , where  $\alpha = 26.890430$  and  $\beta = -9808.402460$ .

Summary of Residuals for Lack of Fit for the Arrhenius Equation

| Source of variation     | df | Sum of squares | Mean squares | F value  | p-value |
|-------------------------|----|----------------|--------------|----------|---------|
| Residual from Arrhenius | 6  | 0.00021        |              |          |         |
| Residual from Model     | 5  | 0.00004        | 0.00001      |          |         |
| Lack of Fit             | 1  | 0.00017        |              | 23.11188 | 0.00485 |

Additional Statistics...  
Sum of Squares of the Error = 0.000033  
Variance of A = 4.291514  
Variance of b = 458610.844716  
Variance in K = 0.040308

First Order Results:

(By convention, projections are rounded and expiration dates are truncated.)  
Arrhenius Projection at 25.0 °C = 42 Months.  
Expiration Date (95.0% CI) at 25.0 °C = 28 Months.

Analysis Complete.

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HISTORY INFORMATION

File Version: 1  
File Status : ACTIVE  
File Name : C:\Program Files (x86)\SLIM\Demo\Accelerated Conditions.SST  
Created : 02 December 2010 at 17:51:28 by Administrator (User ID = 1)  
Last Saved : 26 February 2011 at 23:06:13 by Administrator (User ID = 1)